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Author: Dr. Marc Jorba-Cuscó
Centre National d'Etudes Spatiales (CNES), France, Marc.JorbaCusco@cnes.fr

Dr. Richard Epenoy
Centre National d'Etudes Spatiales (CNES), France, Richard.Epenoy@cnes.fr

LEVERAGING MANIFOLDS OF TORI ASSOCIATED WITH QUASI-SATELLITE ORBITS TO
DESIGN LOW-FUEL MARS-PHOBOS TRANSFERS**Abstract**

Quasi-Satellite Orbits (QSOs) are considered by JAXA's MMX mission, in which CNES is involved [1], for the scientific observation of the Martian moon Phobos prior to landing and sample return operations. These periodic orbits, originally defined in the Mars-Phobos Circular Restricted Three-Body Problem, generally lose periodicity once the eccentricity of Phobos' orbit is taken into account. In this case, QSOs are replaced by quasi-periodic tori [2]. Recent work on MMX project include, amongst many others, station-keeping strategies around QSOs exploiting invariant tori [3]. This study has been carried out considering the elliptical Hill problem.

In this work, we first compute a resonant QSO in the Mars-Phobos Circular Restricted Three-Body Problem. Then, by continuation on the eccentricity of the secondary, we build a family of periodic QSOs parametrized by the eccentricity in the Elliptic Restricted Three-Body Problem. Notice that considering resonant orbits enables us to preserve the periodicity of the QSOs when the eccentricity is non-zero. After reaching the eccentricity of Phobos, we build a family of invariant tori by continuation on the frequency till convergence to the target torus. The tori are computed here in the Elliptic Restricted Three-Body Problem. As a matter of fact, the later model is more precise than the Hill problem at far distance from the secondary and thus more adapted to handle Mars-Phobos transfers. In the next step, we compute the stable invariant manifold emanating from the target torus. Finally, we build nearly-ballistic two-impulse transfers between a parking orbit around Mars and different points on the manifold trying to minimize the total delta-v. Interesting transfer trajectories will be shown allowing for a ballistic capture by Phobos. Here, instead of targeting directly a QSO as done in [4], the spacecraft reaches first the invariant manifold before coasting along the manifold until encountering the target torus.

References

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